

Antiprotons in a Penning Trap: A New Measurement of the Inertial Mass

A thesis presented

by

Robert Lee Tjoelker

to

The Department of Physics

in partial fulfillment of the requirements

for the degree of

Doctor of Philosophy

in the subject of

Physics

Harvard University

Cambridge, Massachusetts

September 1990

©1990 by Robert Lee Tjoelker
All rights reserved.

Abstract

Antiprotons from the Low Energy Antiproton Ring (LEAR) at CERN with a kinetic energy of 5.9 MeV are passed through matter and captured in a cylindrical Penning trap. Using electron cooling, they are brought into thermal equilibrium with the 4 K trapping environment and have been stored for up to 2 months directly establishing the antiproton lifetime to be greater than 103 days.

The inertial masses of the antiproton and proton are compared by direct non-destructive measurements of their oscillatory motions in a Penning trap. An open endcap cylindrical trap produces a high purity quadrupole potential and allows antiprotons to be trapped and cooled. A self-shielding superconducting solenoid compensates the fluctuating magnetic field in the accelerator hall.

The measured mass ratio is $m_{\bar{p}}/m_p = 0.999\,999\,977(42)$. The achieved accuracy of 4.2×10^{-8} is one thousand times more precise than obtained with previous techniques, and is the most stringent test of CPT invariance with baryons. As part of a thorough systematic study, independent comparisons to electrons yield the mass ratios $m_{\bar{p}}/m_{e^-} = 1836.152\,648(89)$ and $m_p/m_{e^-} = 1836.152693(88)$.

Contents

Abstract	i
1 Introduction	1
1.1 Motivation	2
1.2 Mass Spectroscopy in a Penning Trap	5
1.3 Antiprotons: Challenges and Solutions	8
2 Particle Motions in a Penning Trap	9
2.1 Perfect Trap	9
2.2 Imperfect Traps: The Invariance Theorem	13
2.3 Extension to Many Particles	15
3 The Antiproton Trap	17
3.1 Open Endcap Trap	17
3.1.1 A Tunable Quadrupole From Cylindrical Electrodes	18
3.1.2 Construction Issues	25
3.1.3 Calculated Magnetic Bottle	29
3.2 Trap Support and Cryogenic System	32
3.2.1 Description	32
3.2.2 Performance	38
3.3 Shielded Superconducting Magnet	41
3.3.1 Specifications and Field Shimming	41
3.3.2 Self Shielding System	44
3.4 RF Shielding and Grounding	47

4	Cryogenic Antiprotons	50
4.1	Antiprotons provided by CERN	50
4.2	Energy Reduction and Confinement in a Penning Trap	51
4.2.1	Measuring the Antiproton Energy	55
4.2.2	Electron Cooling into the Harmonic Well	58
4.2.3	Reducing the Number of Cooling Electrons	62
4.3	Confinement Lifetime of 4.2 K Antiprotons	64
5	Resistive Detection and Damping	67
5.1	Detection Amplifier	70
5.2	Drive and Detection Scheme and Wiring	77
5.3	Detection Sensitivity	81
5.4	Trap Voltage	83
6	Electrons in the Cylindrical Trap	85
6.1	Observing the Axial Motion	85
6.1.1	Damping Rates and Electron Number	85
6.1.2	Phase Sensitive Detection and Locking the Axial Motion	88
6.1.3	Measurement of the Trap Orthogonalization	90
6.2	Detecting the Cyclotron Motion	91
6.2.1	Microwave Source	91
6.2.2	Anharmonicity Coupling of ν'_c and ν_z	93
6.3	Other Applications with Electrons	97
7	Protons	99
7.1	Loading Protons and Other Positive Ions	99
7.2	Axial Signals	100
7.2.1	Identifying Ions	102
7.2.2	Coupled Cyclotron Observations	104
7.3	Eliminating Contaminant Ions	106
8	Indirect Antiproton Observations: Electron Damping	111
8.1	Observations via Axial Heating of Electrons and Antiprotons	111

8.2	Preliminary Mass Comparison	112
9	Direct Antiproton Observations: Electronic Damping	117
9.1	Direct Cyclotron Detection	117
9.1.1	Simultaneous Measurements of ν'_c and ν_s	119
9.1.2	Cyclotron Measurements vs. Voltage	121
9.2	Phase Sensitive Detection	123
9.2.1	Axial Motion	123
9.2.2	Cyclotron Motion	128
10	Systematic Effects	130
10.1	Deviations From a Stable, Uniform Magnetic Field	130
10.1.1	Homogeneity	130
10.1.2	Field Drift Over Time	133
10.1.3	Fluctuations in the Ambient Field	135
10.2	Deviations From the Pure Quadrupole Electric Field	142
10.2.1	Trap Geometry and Alignment	142
10.2.2	Field Effects From Electrode Potentials	143
10.2.3	Field Effects from the Presence of Other Particles	149
10.3	Particle Energy and Detection	159
10.3.1	Spatial Extent of Particle Motion	159
10.3.2	Detection Effects	169
10.4	Systematic Summary	170
11	The Antiproton, Proton, and Electron Mass Comparison	172
12	Conclusions	182
	References	187

To the Memory of My Father,

Lawrence Earle Tjoelker

Acknowledgements

I am grateful to all the members of the TRAP collaboration who have contributed in many ways to the success of this work. I would like to thank my advisor Jerry Gabrielse for making possible this challenging research opportunity and for his support. My thanks to Luis Orozco, Steve Rolston, Xiang Fei, Hartmut Kalinowsky, Johannes Haas, Tom Trainor, Kris Helmerson, and Bill Kells.

I also wish to thank Ching-Hua Tseng, Loren Haarsma, Joseph Tan, Ben Brown, Won Ho Jhe, and David Phillips for their contributions. Dan Skow, Ron Musgrave, and Heinz Guldenmann constructed many of the components for the cryogenic system, and L.R. DeFeo and E. Sefner machined the traps. I would also like thank Oscar Vilches for his help and enthusiasm. This work would not have been possible without the assistance of many others at Harvard University, the University of Washington, and the LEAR facility at CERN. I thank you all.

Most of all I thank Delinda for her love and patience, and Benjamin and Melissa for reminding me that there are many wonderful things in life other than physics!

List of Figures

- 1.1 Tests of CPT Invariance using baryons, mesons, and leptons. (Data from Review of Particle Properties; Physics Letters B204, April 1988) 4
- 1.2 Previous measurements of the antiproton inertial mass compared to the proton mass. The uncertainty of the new measurement reported in this thesis is approximately 30 times narrower than the dashed line. 6
- 2.1 (a) Schematic representation of the orbit of a charged particle confined in a Penning trap. (b) A scaled representation of the three oscillatory motions for a confined antiproton ($T_z = T_c = 4\text{K}$, $T_m = (\omega_m/\omega_c)4\text{ K}$). 12
- 3.1 The open-endcap compensated cylindrical Penning trap. 19
- 3.2 Electrostatic equipotential field lines in the compensated, open-endcap trap (solid) compared with the field lines for an ideal quadrupole potential (dotted). 24
- 3.3 The open endcap trap showing the assembled split compensation and quad ring electrodes (scale in cm). 26
- 3.4 The extended cylindrical trap mounted from the upper flange of the trap vacuum enclosure (scale in cm). 27
- 3.5 Open-endcap trap with the zeros of $P_4(\cos\theta)$ superimposed. For clarity, the compensation electrodes are rotated azimuthally 45° and the endcap electrodes are truncated. 30
- 3.6 The cryogenic system shown assembled from its modular components. 33

3.7	The Nalorac superconducting magnet with the antiproton trap and cryogenic system inserted into the bore and interfaced to the LEAR beamline. The magnet has a 100 mm diameter bore that can be cooled to 77 Kelvin.	40
3.8	(a) Proton NMR signal mixed down from 249 MHz. (a) Fourier transform of the proton precession from a 1cm diameter spherical sample of acetone. The linewidth represents a field homogeneity of $\Delta B/B=10^{-8}$ over the sample volume. (b) Free Induction Decay of the precessing proton spins.	43
3.9	(a) LEAR and associated experimental areas with the CERN PS shown nearby. The trapping apparatus is located in zone S5. (b) Magnetic field fluctuations in zone S5 resulting from the PS and LEAR cycling their respective magnets. (The typical LEAR cycle takes about 15 minutes and is of opposite polarity shown here). . .	45
3.10	An overall view of the experimental zone showing the Nalorac magnet and the RF shielded region.	48
4.1	(a) The extended trap showing the gold plated aluminum degrader used to reduce the incoming antiproton energy to below 3 kV (scale in cm). (b) Schematic representation of the loading process and the potentials along the axis of the trap.	52
4.2	Antiproton energy scale summarizing our techniques to reduce the antiproton energy by more than 10 orders of magnitude.	53
4.3	Energy spectrum for antiprotons after capture from LEAR into the long trap (a) after a 10 second holdtime and (b) after a 64 hour holdtime. The high voltage ramp as a function of time is superimposed for clarity.	56
4.4	Electron cooling resulting from secondary electrons emitted from the degrader (a) in the long trap, and (b,c) in one-half of the long trap.	57
4.5	Schematic representation of the electron cooling process. The total cooling process occurs in less than 10 seconds.	59

4.6	Antiprotons leaving the harmonic well as a function of well depth and particle number. (a) Annihilations from antiprotons stacked into the harmonic well. (b), (c), and (d) are obtained using only a single shot from LEAR.	60
4.7	Antiproton cyclotron frequency measured on a cloud of 1850 antiprotons over a two month period using techniques described in Chapters 5 and 9.	65
5.1	Schematic circuit for resistive detection and damping of the axial and cyclotron motions of antiprotons (protons) and electrons. . . .	68
5.2	Detection resonant circuit, Field Effect Transistor circuit, and π network used for the 89 MHz cryogenic amplifier.	72
5.3	Voltage induced across the LCR resonant circuit at 4 K for the three amplifiers using the same broadband amplification for (a) the detection of $\nu_z(\bar{p})$, (b) the detection of $\nu_z(e^-)$, and (c) the detection of $\nu'_c(\bar{p})$	76
5.4	Gain and general detection scheme used for square law and phase sensitive detection of the antiproton axial and cyclotron motions ($\nu_z(\bar{p})$ and $\nu'_c(\bar{p})$) and the electron axial motion ($\nu_z(e^-)$).	78
5.5	The trap wired showing all drives, dc lines, and RF filters. The filter values are compromised so that fast ramping of trap potentials can be done in addition to the resonant measurements.	79
6.1	Voltage induced across the axial detection circuit with (a) no electrons loaded, (b) a small number of confined electrons, and (c) a large number of confined electrons.	86
6.2	Locked axial electron responses to the axial and off resonant axial magnetron sideband drive.	89
6.3	The microwave system used to excite the electron cyclotron motion at about 163 GHz.	92

6.4	Locked axial feedback signal as a function of cyclotron drive frequency. Each trace corresponds to a different compensation setting V_{comp}/V_0 . The applied microwave drive strength and sweep rate is constant for all traces.	94
6.5	Cyclotron resonances as observed by monitoring the locked axial feedback signal as a function of cyclotron drive frequency. (a) Hysteresis depending upon sweep direction, and (b) effect of reducing microwave power to resolve on ν'_c	95
7.1	The voltage induced across the resonant tuned circuit at the proton axial frequency with (a) no protons loaded, (b) a small number of protons in the trap, and (c) the response resulting from an extremely large proton cloud. Note the difference with Fig. 6.1 for electrons.	101
7.2	Axial signals of identified positive ions (a) loaded with high energy nested electrons, (b) loaded with lower energy nested electrons, and (c) after applying a noise broadened axial drive sequence to the unwanted ions during loading.	103
7.3	Ion cyclotron resonances of ionized hydrogen, oxygen, and carbon as observed through the axial heating of the proton axial motion. All traces are from the same confined cloud.	105
7.4	Nested trap configurations for energy selection of loaded ions.	108
8.1	Detected axial heating of the electrons (a) and antiprotons (b) as a function of driving on the antiproton cyclotron frequency $\nu'_c(\bar{p})$. (c) The resulting axial antiproton signal resulting from either increased cyclotron drive power or reduced number of electrons.	113
8.2	Antiproton cyclotron frequency as a function of antiproton number as measured through the axial heating of both antiprotons and electrons by collisional coupling.	114

9.1	Direct observations of the antiproton oscillation frequencies on an HP 3561A signal analyzer after being mixed down to approximately 50 kHz. (a) The antiproton modified cyclotron frequency. (b) The antiproton axial frequency.	118
9.2	Antiproton cyclotron frequency as a function of trap voltage and the residuals of the linear fit. Analogous measurements, but with opposite trap polarity, are performed using protons.	122
9.3	Phase sensitive detected axial signal of weakly driven antiprotons.	125
9.4	(a) Highly averaged locked antiproton axial response to drives at $(\nu_z + \nu_{mod})_d$ with the ring potential modulated at ν_{mod} . (b) Trap voltage feedback signal correcting for heating introduced with a weak cyclotron sideband drive at $\nu'_c + \nu_m$	126
9.5	Oscillations in the directly detected ν'_c signal after strong pulsing. .	129
10.1	Antiproton cyclotron frequency as a function of axial location in the trap.	132
10.2	Decay of the magnetic field over several months since magnet energization on December 8 th	134
10.3	(a) Several of the major field fluctuations identified in the experimental hall 1.5 m from the trap. (b) Amplified measurement of fluctuations during a quiet period with the accelerator magnets off. (c) Expanded view of the PS cycle.	136
10.4	Magnetic Fluctuations from the CERN Proton Synchrotron superimposed on a LEAR deceleration cycle. (a) Measured with a magnetometer outside of the magnet and (b) measured with an identical magnetometer inside the self shielding solenoid.	138
10.5	The magnetic field shift due to bending magnet S4-BHN01 at the trap center as measured by a shift in the electron cyclotron resonance.	139
10.6	Antiproton cyclotron frequency as a function of trap compensation.	145
10.7	Antiproton and Proton axial and cyclotron resonances showing the effect of reversing the trapping potential.	147

10.8	Axial shift for protons when reducing particle number in the trap. The axial signal (a) before and (b) after a drive a dip procedure to reduce proton number. The axial frequency increases for reduced particle number.	150
10.9	Axial shift for antiprotons as a function of the drive and dip procedure to reduce the antiproton number in the trap.	151
10.10(a)	The dependence of the magnetron frequency $\nu_z^2/2\nu'_c$ on particle number. (b) The dependence of the modified cyclotron frequency ν'_c on particle number.	152
10.11	Measured antiproton cyclotron frequencies as a function of number of antiprotons in the trap.	153
10.12(a)	Antiproton and proton cyclotron frequency ν'_c as a function of applied trapping voltage. (b) Blown up view of the extrapolated free space cyclotron frequency compared to measurments using the invariance theorem $\nu'_c + \nu_z^2/2\nu'_c$. A potential offset is evident. . . .	156
10.13(a)	Three measurements of the antiproton cyclotron frequency directly observed from a segment of the ring electrode. (b) Damping of the cyclotron center of mass motion as observed with a square law detector centered at $\nu_c(\bar{p})$	161
10.14	The cyclotron frequency shift $\Delta\nu'_c$ of a single antiproton as a function of the cyclotron radius due to special relativity, a magnetic bottle (+1 G/cm ²), or trap anharmonicity ($C_4 \leq -7.8 \times 10^{-4}$). The shift due to C_4 can be in either direction depending upon the compensation of the trapping potentials.	162
10.15	Axial shift for a fixed number of protons as a function of temperature in the axial motion	164
10.16	The axial and cyclotron motions are approximately in thermal equilibrium.	166
10.17	Large amount of heat in the cyclotron motion while the axial motion remains cool.	167

10.18	The cyclotron motion is partially damped and the axial motion remains cold.	168
11.1	(a) Series of cyclotron measurements for antiprotons, protons and electrons over time. The 5 three way comparison sets are shown. (b) Expanded view of comparison set #5.	174
11.2	(a) The data in Fig. 10.1 with the magnetic field drift subtracted out. (b) The residuals about the least squares fit showing the scatter of the antiproton measurements taken over the 10 day period. . . .	175
11.3	Mass comparisons $m_{\bar{p}}/m_p$, $m_{\bar{p}}/m_p$, and m_p/m_{e^-} . The weighted average and assigned uncertainty is shown in dashed lines.	178
12.1	Measurements of the ratio of antiproton to proton inertial masses. Our new measurement shown on the right is an increase in accuracy of 1000.	183
12.2	(a) Previous Measurements of the proton-electron mass ratio with our new measurement performed in the new open endcap trap. It is in agreement with the most recent, higher precision measurement by VanDyck et. al. . (b) Our new measurement of the antiproton-electron mass ratio.	184